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ABSTRACT

In transition-metal dipnictides $TmPn_2$ (Tm = Ta and Nb; Pn = P, As, and Sb), the origin of extremely large magnetoresistance (XMR) is yet to be studied by the direct visualization of the experimental band structures. Here, using angle-resolved photoemission spectroscopy, we map out the three-dimensional electronic structure of NbAs₂. The open-orbit topology contributes to a non-negligible part of the Fermi surfaces (FSs), like that of the isostructural compound MoAs₂, where the open FS is proposed to likely explain the origin of XMR. We further demonstrate the observation of open characters in the overall FSs of W₂As₃, which is also a XMR semimetal with the same space group of C12/m1 as the $TmPn_2$ family and MoAs₂. Our results suggest that the open-orbit FS topology may be a shared feature between XMR materials with the space group of C12/m1 and, thus, could possibly play a role in determining the corresponding XMR effect together with the electron-hole compensation.

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Serving as a fertile ground for topological quantum states and a promising candidate for device applications, the topological semimetal (TSM) has inspired great research interest in the community.^{1–23} Different from topological insulators,²⁴ the bulk states and topological

surface states in TSMs have more novel forms.^{9–14,22,23,25–27} With such diverse electronic properties, TSMs exhibit many unusual magneto-transport phenomena, such as linear transverse magnetoresistance (MR) and negative longitudinal MR in Dirac/Weyl semimetals^{28–34}

and extremely large transverse MR (XMR) in nonmagnetic semimetals.^{35–40} Fully exploring the MR-related phenomena can not only facilitate understanding the physics in TSMs but also promote the development of practical applications like magnetic memory/sensor devices.

Recently, since the discovery of the quadratic XMR effect in WTe2,41 significant research interest has been stimulated in understanding its microscopic mechanism and exploring new XMR materials. A series of nonmagnetic semimetals with XMR have been established, like transition-metal dipnictides $TmPn_2$ (Tm = Taand Nb; Pn = P, As, and Sb),^{42–63} LnX (Ln = La, Y, Nd, or Ce; X = Sb/Bi),^{64–72} ZrSiS family,^{73–75} MoAs₂,^{76–78} W₂As₃,^{79–81} PtBi₂,⁸² PtSn₄,⁴⁰ WP₂,⁸³ etc. So far, several scenarios have been proposed to explain the XMR behavior, including nontrivial band topology,⁶⁴ electron-hole compensation,^{41,84} open-orbit Fermi surface (FS) topology,⁷⁶ forbidden backscattering at zero field,⁸⁵ and field-induced FS changes.⁴² However, when looking back, one finds that the study of $TmPn_2$ family is still at the early stage it was while it ignited substantial works. The lack of experimental electronic structure study is the main problem because the MR behavior in semimetals is believed to intimately correlate with the underlying electronic structure. Previous angle-resolved photoemission spectroscopy (ARPES)⁷⁶ and quantum oscillations⁷⁸ measurements on the isostructural compound MoAs₂ suggest that the origin of XMR may be attributed to the dominant open-orbit FS topology. In order to gain insight into the mechanism of the XMR in these isostructural materials, it is critical to experimentally reveal the band structure of other representative compounds.

Utilizing ARPES, here, we present the electronic structure study on XMR semimetals NbAs₂ and W₂As₃, both with the space group of $C12/m1.^{46,80}$ Unlike most XMR materials whose FSs are usually dominated by closed pockets, we uncover that the band structures of NbAs₂ and W₂As₃ host non-negligible open-orbit FS topologies in the threedimensional (3D) momentum space, where the ripple-shaped bulk FSs show open character along two perpendicular high-symmetry directions. Our results, combining with the previously studied $MoAs_2$,^{76,78} suggest that the open FS may be a shared feature between XMR compounds with the space group of C12/m1 and, thus, could possibly make a contribution to the corresponding XMR behavior together with the electron–hole compensation.

High-quality single crystals of NbAs2 and W2As3 were obtained by chemical vapor transport methods.^{46,80} ARPES measurements of NbAs₂ and W₂As₃ were performed at the Dreamline beamline of the Shanghai Synchrotron Radiation Facility and the beamline 5-2 of the Stanford Synchrotron Radiation Lightsource (SSRL) using photons with linear horizontal polarization, respectively. The energy and angular resolutions were set to better than 15 meV and 0.1°, respectively. Samples were cleaved in situ, yielding flat mirrorlike surfaces. During the measurements, the temperature was kept at 20 K, and the pressure was maintained better than 5×10^{-11} Torr. The first-principles calculations were performed with Vienna ab initio Simulation Package⁸ for W2As3. A plane wave basis up to 400 eV was employed in the calculation. The Perdew-Bruke-Ernzerhof parametrization of generalized gradient approximation to the exchange correlation functional⁸⁸ was employed in the calculation. The electronic structure was calculated for the conventional cell with $4 \times 12 \times 5$ Γ -centered k mesh. The tight-binding (TB) Hamiltonian was obtained by fitting the densityfunctional theory band structures using the maximally localized Wannier function method.⁸⁹ The electronic structure of (100) surface was calculated for the conventional cell with the surface Green's function method⁹⁰ using the TB Hamiltonian after symmetrization.⁹

Figure 1 illustrates the overall physical properties of NbAs₂ and W_2As_3 crystals. The crystal structures with the monoclinic C12/m1 space group are presented in Fig. 1(a). The corresponding bulk primitive Brillouin zone (BZ) and conventional BZs of $(20\overline{1})$ and (100)



FIG. 1. Single crystals of NbAs₂ and W_2As_3 . (a) Schematic crystal structures of NbAs₂ and W_2As_3 . (b) Sketches of the 3D primitive BZ and conventional BZs of (201) and (100) surfaces of monoclinic C12/m1 space group structure. (c) XRD pattern on the NbAs₂ (201) surface. Inset: picture of a NbAs₂ crystal. (d) Same as (c) on the W_2As_3 (200) surface. Inset: picture of a W_2As_3 crystal. (e) Temperature dependence of the resistivity (ρ_{xx}) of NbAs₂ under different magnetic fields, where *I* is parallel to the *b* axis and *B* is perpendicular to the *bc* plane. (g) and (h) Core-level photoemission spectra of NbAs₂ and W_2As_3 measured with 100- and 200-eV photons, respectively.

surfaces are shown in Fig. 1(b). Single crystal x-ray diffraction (XRD) patterns in Figs. 1(c) and 1(d) demonstrate the crystal surfaces of our measured samples: the $(20\overline{1})$ plane of NbAs₂ and the (200) plane of W₂As₃. The temperature dependence of resistivity under various magnetic fields [Figs. 1(e) and 1(f)] agrees with the previous studies on $TmPn_2$ and W₂As₃.^{43,44,48,79,81} As most nonmagnetic XMR semimetals,^{64,65} the temperature-dependent ρ_{xx} exhibits a typical metallic behavior under zero field, and upon turning on the magnetic field, the resistivity prominently increases and forms a plateau at low temperatures ultimately. The quadratic MR of 1.0×10^5 % and 6.9×10^4 % with the magnetic field up to 14T can be found in our earlier transport studies on NbAs2⁴⁶ and W2As3,⁸⁰ respectively. The characteristic peaks of Nb, W, and As elements are resolved in the core-level photoemission spectra in Figs. 1(g) and 1(h), further verifying the chemical compositions of NbAs₂ and W₂As₃ samples. It is noted that the Nb-4p peaks are rather weak in Fig. 1(g), which could be due to the dramatic suppression of the photoionization cross sections of Nb 4p in this photon energy regime as compared with W 4f and As 3d.

In earlier theoretical calculations,^{45,79} the overall bulk band structures of NbAs₂ and W₂As₃ indicate the coexistence of electron- and hole-like bands crossing the Fermi level (E_F). This appears to support the carrier compensation mechanism suggested by the transport measurements based on the classic two-band model.^{48,79} To gain more insight into the origin of the XMR behavior,^{46,80} we systematically investigate their electronic structures by ARPES. As shown in Figs. 2(a) and 2(b), one can see that the in-plane FSs of both compounds exhibit periodic modulations along the k_x and k_y directions. Notably, the ripple-shaped FS contours elongated along the k_v directions show no signature of closure, behaving as the open FSs, in sharp contrast to the complicated closed ones along the $k_x = 0$ lines $(\overline{\Gamma} - \overline{M})$. We further carry out photon-energy-dependent measurements along the $\overline{\Gamma} - \overline{N}$ directions. In Figs. 2(c) and 2(d), the noticeable dispersions of overall band structure as a function of photon energy demonstrate the bulk origin of our observations. Moreover, one obtains that the rippleshaped FSs do not close along the k_z directions either. The modulation behavior of the open FSs in each compound is found to be equivalent along the k_v and k_z directions. The presence of open characters in 3D FS topologies of NbAs2 and W2As3 is similar to the isostructural MoAs₂,⁷ implying that the open FS may be a shared feature between XMR materials with the space group of C12/m1.

The near- $E_{\rm F}$ ARPES spectra of NbAs₂ are measured along cuts #a and #b in Fig. 2(a). As shown in Figs. 3(a) and 3(c), the conduction band region is composed of alternate electron-like bands, which define the neighboring open FS sheets, and linearly dispersive hole-like bands corresponding to the closed pockets along the $\overline{\Gamma} - \overline{M}$ direction. By tracing the peak positions of momentum distribution curves (MDCs)



FIG. 2. 3D FS topologies of NbAs₂ and W₂As₃. (a) Constant-energy ARPES image of NbAs₂ by integrating the photoemission intensity within $E_F \pm 40$ meV measured with 100-eV photons. Cuts #a and #b indicate the locations of the experimental band structures in Fig. 3. (b) Same as (a) of W₂As₃. The red solid curves show the (201)- and (100)-projected BZs of NbAs₂ and W₂As₃, respectively. (c) ARPES intensity plot of NbAs₂ in the $h\nu$ - k_x plane at E_F , with k_x oriented along the $\overline{\Gamma} - \overline{N}$ direction. (d) Same as (c) of W₂As₃. The modulation of open FS is indicated by red open circles.



FIG. 3. Near- E_F band structure of NbAs₂. (a) and (b) ARPES intensity plot and corresponding MDCs along the $\overline{\Gamma} - \overline{N}$ direction [cut #a in Fig. 2(a)] recorded at $h\nu = 100 \text{ eV}$, respectively. (c) and (d) Same as (a) and (b) along cut #b in Fig. 2(a). (e) and (f) Same as (a) and (b) taken with 66-eV photons. The blue dashed lines in (d) and (f) are extracted peak positions, indicating the linearly dispersing bands around $k_x \sim 0$.

in Figs. 3(b) and 3(d), one can observe the modulation of multiple linear dispersions (around $k_x \sim 0$) along the k_y direction. We further record the band structure along cut #a at $h\nu = 66$ eV. The overall band dispersions [Figs. 3(e) and 3(f)] are analogous to that along cut #b taken with 100-eV photons [Figs. 3(c) and 3(d)]. This similarity demonstrates that, including the open FSs, the modulation behavior of the electronic structure in NbAs₂ is equivalent along the k_v and k_z directions. Regardless of the FS topology, the observation of both electronand hole-like bulk bands near $E_{\rm F}$ seems to favor the electron-hole compensation picture proposed in theoretical calculations⁴⁵ and transport studies,⁴⁸ which will be discussed later. It is worth noting that the recent optical spectroscopy experiments on NbAs2 have demonstrated the electromagnetic signature of dispersive Dirac nodal lines with spin-orbit coupling gaps.^{92,93} The corresponding fermiology and band dispersions show similarities to that of the open FSs observed here. More unique properties associated with the open orbits, thus, merit further explorations.

We then turn to study the band structure of W₂As₃. As illustrated in Fig. 2(d), the photon energies of 100 and 70 eV corresponding to the high-symmetry k_z planes are used for the measurements. Because of the same modulation behavior of the open FSs along the k_y and k_z directions, the neighboring open FSs (in the k_x - k_y plane), for example, at $k_y = 0$ ($\overline{\Gamma} - \overline{N}$), are concave and convex with respect to the BZ boundary ($\overline{N} - \overline{X}$) in the 100- and 70-eV FS mappings, respectively. Here, in Fig. 4(c), we artificially align the concave section of 70-eV mapping along $k_y = 0$ ($\overline{\Gamma} - \overline{N}$) as in Fig. 2(b) to unify the momentum cut assignment. As indicated by cuts #1-#5 in Fig. 4(c), we record the ARPES spectra near E_F along some representative momentum cuts on the ripple-shaped FSs. The intensity plots measured at $h\nu = 100$ and 70 eV are shown in Figs. 4(a) and 4(b), respectively. The band structures around $\overline{\Gamma}$, \overline{M} , and along $k_x = 0$ ($\overline{\Gamma} - \overline{M}$) are composed of multiple hole-like bands, forming complicated FS pockets [Figs. 2(b) and 4(c)]. In contrast, as highlighted by black arrows in Figs. 4(a) (cut #3) and 4(b) (cuts #2 and #3), the relatively simple band structures, which define the ripple-shaped open FSs, dominate around the BZ boundary $(\overline{N} - \overline{X})$. Moreover, from cuts #1 to #5, a band crossing formed by the dispersions of neighboring open FSs always exists. Accordingly, as illustrated in the spectra along cuts #6 [indicated in Fig. 4(c) in Figs. 4(a) and 4(b), the "nodal-line"-like behavior is observed in both two k_z planes. As a result, these band crossings seem to constitute a "nodal surface" normal to the k_x - k_y plane. As suggested by an earlier theoretical study on the nodal-surface semimetals, one necessary requirement for a topologically protected nodal surface is that the space-time inversion symmetry is violated.⁹⁴ However, the space inversion symmetry P preserves in the space group of C12/m1,⁷⁶ and there is no magnetic order revealed in W_2As_3 ,⁷⁹ ⁸¹ thus the $P \cdot T$ symmetry is present. The "nodal surface" here is not topological and could be caused by band structure effects, such as band folding effect, which calls for future investigations. We further carry out the TB calculations on the (100) surface of W2As3 using the surface Green's function method. As shown in Figs. 4(d) and 4(e), one can obtain that the calculations within the first BZ well reproduce the overall electronic structures in experiment, especially the ones associated with the open characters.

The previous transport measurements have suggested the critical role of electron–hole compensation in determining the quadratic XMR behavior in NbAs₂ and W₂As₃.^{48,79,80} Although the carrier compensation scenario can be well applied in many XMR semimetals with closed FS trajectories based on the two-band model,^{41,65,84,95} its availability in XMR materials with non-negligible open FS characters is yet to be established.⁹⁶ In materials with closed FSs, upon applying the magnetic field, all electron and hole orbits under Lorentz force are



FIG. 4. Near- E_F band structure of W₂As₃. (a) ARPES intensity plots along cuts #1–#6 in (c) taken with 100-eV photons. (b) Same as (a) recorded at $h\nu = 70$ eV. The red dashed curves in cuts #1–#5 are guides to the eye for the band crossings around the BZ boundary $(\overline{N} - \overline{X} - \overline{N})$. The black arrows indicate the band dispersions defining the open FSs. The red dashed curves in cuts #6 are guides to the eye for the "nodal lines." (c) Constant-energy ARPES image of W₂As₃ by integrating the photoemission intensity within $E_F \pm 40$ meV measured with 70-eV photons. Cuts #1–#6 indicate the locations of the experimental band structures in (a) and (b). (d) Calculated FS contours of the (100) surface of W₂As₃. (e) Calculated band structure along the $\overline{X} - \overline{M} - \overline{X}$ direction [blue solid line in (d)] of the (100) surface.

closed ones. The MR tends to saturate at high magnetic fields unless the electron and hole carriers are compensated, and the dominant closed character of FSs is necessary for the XMR related to the carrier compensation mechanism. In contrast, when the open orbits dominate the FS topology perpendicular to the magnetic field, the MR would increase as H^2 without any sign of saturation, regardless of whether or not the balance between electron and hole carriers.97 The distinct velocities of electrons in the plane perpendicular to the magnetic field are found to be the cause of these different behaviors.98,99 Recently, the open-orbit FS topology has been suggested as a possible self-contained and dominant mechanism of the XMR in isostructural compound MoAs₂.⁷⁶ Nevertheless, by comparing with the case in MoAs₂, where the open FS is reported to be dominant of the overall electronic structures,^{76,78} our observations in NbAs₂ and W₂As₃ reveal that the open and closed features each defines a non-negligible part of FSs. Therefore, only considering the electron-hole compensation is inadequate, a collaboration between the open FS and the carrier compensation may explain the origin of the quadratic XMR in these two compounds. The open FS scenario may be taken into account in a broad range of XMR semimetals with the space group of C12/m1.

In summary, we have studied the electronic structure of XMR semimetals NbAs₂ and W₂As₃ by ARPES experiments. The rippleshaped bulk FSs do not close along two perpendicular high-symmetry directions, showing the open-orbit FS topologies similar to that of isostructural MoAs₂.^{76,78} Our results suggest that the open FS may be a shared feature between XMR materials with the space group of C12/m1 and, thus, could possibly collaborate with the electron-hole compensation to solve the origin of the corresponding XMR effect.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts to disclose.

Author Contributions

R.L., Y.Y.W., L.X.Z., C.C.X., and M.L. contributed equally to this work.

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding authors upon reasonable request.

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